

Package: FrailtyCompRisk (via r-universe)

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Title Competing Risks Models for Multi-Center Survival Data with Frailty

Version 0.1.1

Description Implements methods for analyzing competing risks data in multi-center survival studies using frailty models. The approach relies on a mixed proportional hazards model for the sub-distribution, allowing for cluster-specific random effects. The package provides tools for model estimation with or without frailty using Maximum Likelihood (ML) and Restricted Maximum Likelihood (REML). It supports flexible modeling of between-center heterogeneity and is particularly suited for multi-center clinical trials or registries. Core features include data simulation, likelihood computation, cluster-dependent censoring options, and testing of frailty effects. For methodological details, see Katsahian et al. (2006) <[doi:10.1002/sim.2684](https://doi.org/10.1002/sim.2684)>.

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| | |
|-------------------|--|
| check_data_format | <i>Check the Format of a Data Frame for Multicentre Competing Risks with Frailty</i> |
|-------------------|--|

Description

Validates whether the submitted data frame is correctly structured for the analysis of multicentre competing risks with frailty.

Usage

```
check_data_format(df)
```

Arguments

df A data frame to be checked.

Value

TRUE if df has the expected structure. Otherwise, the function stops with an error describing the formatting issue.

Examples

```

n_cov = 1
n_cluster = 5
n_per_cluster = 100
n = n_cluster * n_per_cluster
a1 = 0
b1 = 1
G <- rep(1:n_cluster, each = n_per_cluster)
Z <- matrix(runif(n * n_cov, a1, b1), ncol = n_cov)
df = simulate_data(
  G,
  Z,
  prop = 0.6,
  beta = c(0),
  theta = 0.01,
  cens = TRUE,
  pcens = 0.25,
  tau = 0
)
check_data_format(df)

```

compute_M_optimized *Compute the Weight Matrix M (Optimized)*

Description

This function computes the matrix of inverse probability of censoring weights (IPCW), used in multicenter competing risks models with frailty. It supports both Kaplan-Meier and Nelson-Aalen estimators for the censoring distribution.

Usage

```
compute_M_optimized(times, status, f, u_bis, clusters)
```

Arguments

| | |
|----------|---|
| times | A numeric vector of observed times (events or censoring). |
| status | A numeric vector of status indicators (0 = censored, 1 or 2 = cause of failure). |
| f | A string, either "KaplanMeier_Censoring_vectorized" or "Nelson_Censoring_vectorized", specifying the method to estimate the censoring distribution. |
| u_bis | A numeric vector of cluster-level random effects (used only if f == "Nelson_Censoring_vectorized"). |
| clusters | A vector indicating cluster membership for each subject (same length as times). |

Details

- If `f == "KaplanMeier_Censoring_vectorized"`, then `u_bis` is ignored.
- The weight matrix accounts for pairwise contributions, depending on event times and causes.

Value

A square matrix `M` of size $N \times N$, where `M[i, j]` is the IPCW weight between subject `i` and subject `j`.

See Also

[KaplanMeier_Censoring_vectorized\(\)](#), [Nelson_Censoring_vectorized\(\)](#), [create_G_function\(\)](#)

`create_G_function` *Create Step Function for Estimated Survival (G)*

Description

This function creates a right-continuous step function (vectorized) based on estimated values of the censoring survival function at given unique times.

Usage

```
create_G_function(unique_times, G_vals)
```

Arguments

`unique_times` A numeric vector of increasing unique times (e.g., censoring times).

`G_vals` A numeric vector of the same length as `unique_times`, corresponding to estimated values of the survival function at each time.

Details

The resulting function can be used to evaluate $G(t)$ for any vector of time points.

Value

A function `G(t)` that can be evaluated on a numeric vector of time points.

KaplanMeier_Censoring_vectorized
Kaplan-Meier Estimator for Censoring Distribution (Vectorized)

Description

Computes the Kaplan-Meier estimator of the censoring distribution at given time points.

Usage

```
KaplanMeier_Censoring_vectorized(times, status, unique_times)
```

Arguments

times A numeric vector of observed times.
status A numeric vector of status indicators (0 = censored, >0 = event).
unique_times A numeric vector of time points at which to evaluate the estimator.

Value

A numeric vector of estimated survival probabilities at each unique time.

logLikelihood_1 *Log-Likelihood Contribution for Cause 1*

Description

Computes the contribution to the log-likelihood from individuals who experienced event type 1, using a weighting matrix W and an IPCW matrix M.

Usage

```
logLikelihood_1(status, M, W)
```

Arguments

status A numeric vector indicating the event type: 0 for censored, 1 for cause 1, 2 for other causes.
M A numeric matrix (usually computed with `compute_M_optimized`), representing IPCW weights between individuals.
W A sparse matrix (e.g., of class `dgCMatrix` from the **Matrix** package) representing estimated weights or hazards.

Details

For each individual i such that `status[i] == 1`, the function computes:

$$\log W_{ii} - \log \left(\sum_j M_{ij} W_{ij} \right)$$

and sums this across all such individuals.

Value

A numeric scalar: the log-likelihood contribution from all individuals who failed from cause 1.

See Also

[compute_M_optimized\(\)](#), [Matrix::Matrix](#)

logLikelihood_2

Compute Log-Likelihood Penalty for Random Effects

Description

This function computes the second component of the log-likelihood (penalty term) associated with the random effects (frailty terms) in a mixed-effects model.

Usage

```
logLikelihood_2(u, theta, K)
```

Arguments

| | |
|--------------------|---|
| <code>u</code> | A numeric vector of length K containing the random effects (frailties). |
| <code>theta</code> | A positive numeric scalar, representing the variance component of the random effects. |
| <code>K</code> | An integer representing the number of clusters (i.e., the length of <code>u</code>). |

Details

The penalty is derived from the Gaussian assumption on the random effects and involves both the dimension of the random effects vector and the variance parameter `theta`.

Value

A numeric scalar representing the log-likelihood penalty contribution from the random effects.

Description

Performs maximum likelihood estimation (MLE) for the effect of covariates on the cause-specific hazard function of cause 1 in a competing risks framework.

Usage

```
ML_CompRisk(data, max_iter = 100, tol = 1e-06)
```

Arguments

| | |
|-----------------------|---|
| <code>data</code> | A data frame containing: times Observed survival or censoring times. status Event indicator: 0 = censored, 1 = cause 1 (event of interest), 2+ = other causes. Covariates All columns from the 4th onward are considered as covariates. |
| <code>max_iter</code> | Maximum number of Newton-Raphson iterations (default = 100). |
| <code>tol</code> | Convergence tolerance for the change in parameter estimates (default = 1e-6). |

Details

The function fits a Cox-type model for the subdistribution hazard of cause 1, treating all other causes (including censoring) as censored (i.e., `status != 1` becomes 0). It uses a Newton-Raphson procedure to maximize the partial likelihood.

The design matrix is reordered internally by event time to facilitate risk set computation.

Value

A named list with one element:

beta A numeric vector of estimated regression coefficients for the subdistribution hazard of cause 1. Each coefficient represents the log effect of the corresponding covariate on the subdistribution hazard.

See Also

[Repl_Cox_frailty](#), [ML_Cox](#), [logLikelihood_1](#)

Examples

```

data <- data.frame(
  times = c(0.099, 0.006, 0.260, 0.151, 0.262,
            0.019, 0.026, 0.241, 0.017, 0.195,
            0.007, 0.057, 0.241, 0.132, 0.044,
            0.242, 0.416, 0.096, 0.172, 0.015),
  status = c(1, 0, 1, 1, 0,
             0, 0, 0, 0, 0,
             0, 0, 0, 0, 0,
             0, 0, 0, 0, 0),
  clusters = c(1,1,1,1,1,
               1,1,1,1,1,
               2,2,2,2,2,
               2,2,2,2,2),
  V1 = c(0.720, 0.289, 0.382, 0.995, 0.045,
          0.048, 0.042, 0.810, 0.964, 0.781,
          0.443, 0.303, 0.902, 0.596, 0.462,
          0.521, 0.656, 0.164, 0.261, 0.635)
)
beta_hat <- ML_CompRisk(data)

```

ML_Cox

Maximum Likelihood Estimation for the Cox Model (Optimized)

Description

This function computes the maximum likelihood estimates of the regression coefficients in the Cox proportional hazards model using Newton-Raphson iterations.

Usage

```
ML_Cox(data, max_iter = 100, tol = 1e-06)
```

Arguments

| | |
|-----------------------|--|
| <code>data</code> | A data frame with columns: times, status, and covariates starting from the 4th column. |
| <code>max_iter</code> | Maximum number of iterations (default = 100). |
| <code>tol</code> | Convergence tolerance for the Euclidean norm (default = 1e-6). |

Value

A named list with one element:

beta A numeric vector of estimated regression coefficients in the Cox proportional hazards model. Each coefficient represents the log hazard ratio associated with the corresponding covariate.

 Nelson_Censoring_vectorized

Nelson-Aalen Estimator of Censoring Distribution (Vectorized)

Description

Computes the estimated censoring survival probabilities using a Nelson-Aalen-type estimator, accounting for shared frailty through a cluster-specific random effect.

Usage

```
Nelson_Censoring_vectorized(times, unique_times, status, clusters, u_bis)
```

Arguments

| | |
|--------------|---|
| times | A numeric vector of observed times. |
| unique_times | A numeric vector of distinct, sorted time points. |
| status | A numeric vector where 0 indicates censoring. |
| clusters | A vector indicating the cluster/group for each observation. |
| u_bis | A numeric vector of cluster-specific random effects (e.g., frailty values). |

Value

A numeric vector of estimated censoring survival probabilities for each individual.

 Parameters_estimation *Unified Interface for Parameter Estimation in (Competing Risks) Frailty Models*

Description

Provides a unified wrapper to estimate model parameters under four different modeling strategies:

- Competing risks with shared frailty for cause 1 ("CompRisk_frailty")
- Competing risks without frailty for cause 1 ("CompRisk")
- Standard Cox model with shared frailty ("Cox_frailty")
- Standard Cox model without frailty ("Cox")

Usage

```
Parameters_estimation(
  data,
  method = "CompRisk_frailty",
  cluster_censoring = FALSE,
  max_iter = 300,
  tol = 1e-06,
  threshold = 1e-06
)
```

Arguments

| | |
|--------------------------------|--|
| <code>data</code> | A data frame containing at least the following columns: times Event or censoring times. status Event indicator: 0 = censored, 1 = event of interest, >1 = other types (for competing risks). clusters Cluster/group variable (e.g., center ID). covariates (Optional) Additional covariates from the 4th column onward. |
| <code>method</code> | Character string indicating the estimation method. One of: <ul style="list-style-type: none"> • "CompRisk_frailty" (default): Competing risks model for cause 1 with shared frailty. • "CompRisk": Competing risks model for cause 1 without frailty. • "Cox_frailty": Cox proportional hazards model with shared frailty. • "Cox": Standard Cox proportional hazards model. |
| <code>cluster_censoring</code> | Logical. If TRUE, adjusts for cluster-specific censoring. Only applicable when <code>method = "CompRisk_frailty"</code> (default = FALSE). |
| <code>max_iter</code> | Maximum number of iterations for the selected model estimation (default = 300). |
| <code>tol</code> | Convergence tolerance (default = 1e-6). |
| <code>threshold</code> | Lower bound for the frailty variance parameter θ . If the estimated value falls below this threshold, frailty is considered negligible (default = 1e-5). |

Details

This wrapper allows seamless switching between various modeling frameworks. It automatically calls:

- `Reml_CompRisk_frailty` for "CompRisk_frailty"
- `ML_CompRisk` for "CompRisk"
- `Reml_Cox_frailty` for "Cox_frailty"
- `ML_Cox` for "Cox"

Data format is validated via the helper function `check_data_format`. An error is raised if input format is invalid or if `cluster_censoring` is used with an incompatible method.

Value

A named list whose structure depends on method. For "CompRisk" and "Cox", the returned list contains:

beta Numeric vector of estimated regression coefficients.

For "CompRisk_frailty" and "Cox_frailty", the returned list may contain:

beta Numeric vector of estimated fixed-effect coefficients.

u Numeric vector of estimated cluster-specific frailties.

theta Estimated frailty variance parameter.

p_value P-value for testing the null hypothesis of no frailty effect.

Returns NULL if estimation fails.

See Also

[Reml_CompRisk_frailty](#), [Ml_CompRisk](#), [Reml_Cox_frailty](#), [Ml_Cox](#), [check_data_format](#)

Examples

```
data <- data.frame(
  times = c(4, 6, 10, 12, 3),
  status = c(1, 0, 2, 1, 0),
  clusters = c(1, 1, 2, 2, 3),
  x1 = rnorm(5),
  x2 = sample(0:1, 5, replace = TRUE)
)
result <- Parameters_estimation(data, method = "CompRisk_frailty")
result$beta
```

Reml_CompRisk_frailty *REML Estimation for Cause 1 in a Competing Risks Model with Shared Frailty*

Description

Fits a cause-specific hazard model for cause 1 in a competing risks framework using restricted maximum likelihood (REML) with a shared frailty term for clusters.

Usage

```
Reml_CompRisk_frailty(
  data,
  cluster_censoring = FALSE,
  max_iter = 300,
  tol = 1e-06,
  threshold = 1e-05
)
```

Arguments

| | |
|--------------------------------|--|
| <code>data</code> | A data frame with at least the following columns: times Observed times to event or censoring. status Event type: 0 = censored, 1 = cause of interest, >1 = other competing risks. clusters Cluster membership (e.g., centers or subjects). covariates (Optional) Columns from the 4th onward are used as covariates. |
| <code>cluster_censoring</code> | Logical. If TRUE, accounts for center-specific censoring using a frailty model on censoring times. Default is FALSE. |
| <code>max_iter</code> | Maximum number of iterations for the Newton-Raphson algorithm (default = 300). |
| <code>tol</code> | Convergence tolerance for the likelihood and frailty variance (default = 1e-6). |
| <code>threshold</code> | Lower bound for the frailty variance parameter θ . If the estimated value falls below this threshold, frailty is considered negligible (default = 1e-5). |

Details

The function fits a proportional hazards model for cause 1, accounting for unobserved heterogeneity via a shared frailty term on clusters. When `cluster_censoring = TRUE`, a frailty-adjusted survival curve is used to correct for informative censoring using either a Kaplan-Meier or Nelson-Aalen-based estimator.

If the estimated frailty variance θ becomes smaller than the provided `threshold`, the model reverts to a standard Cox model for cause 1 using [ML_CompRisk](#).

Value

A list with:

beta Estimated regression coefficients for the cause 1 hazard.

u Estimated cluster-specific random effects (frailties).

theta Estimated frailty variance.

p_value P-value testing the null hypothesis $H_0 : \theta = 0$.

See Also

[ML_CompRisk](#), [Reml_Cox_frailty](#), [logLikelihood_1](#), [compute_M_optimized](#)

Examples

```
data <- data.frame(
  times = c(4, 6, 10, 12, 3),
  status = c(1, 0, 2, 1, 0),
  clusters = c(1, 1, 2, 2, 3),
  x1 = rnorm(5),
  x2 = sample(0:1, 5, replace = TRUE)
)
```

```

result <- Repl_CompRisk_frailty(data)
result$beta
result$p_value

```

| | |
|------------------|--|
| Repl_Cox_frailty | <i>Cox Model with Random Frailty (REML Estimation)</i> |
|------------------|--|

Description

Estimates the regression coefficients, random effects, and frailty variance θ in a Cox proportional hazards model with shared frailty using Restricted Maximum Likelihood (REML).

Usage

```
Repl_Cox_frailty(data, max_iter = 300, tol = 1e-06, threshold = 1e-05)
```

Arguments

| | |
|-----------|---|
| data | A data frame containing: <ul style="list-style-type: none"> • times: observed survival or censoring times, • status: event indicator (1 = event, 0 = censored), • clusters: cluster identifiers (e.g., center, group), • covariates from column 4 onward. |
| max_iter | Maximum number of Newton-Raphson iterations (default = 300). |
| tol | Tolerance for convergence (default = 1e-6). |
| threshold | Lower bound for the frailty variance parameter θ . If the estimated value falls below this threshold, frailty is considered negligible (default = 1e-5). |

Details

The function uses a REML-based Newton-Raphson approach to estimate the parameters. A penalized likelihood including a log-likelihood contribution for the frailty variance θ is maximized.

The hypothesis test of $H_0 : \theta = 0$ is based on a Wald-type statistic. A high p-value (e.g. > 0.05) may indicate that the random effects (frailties) are negligible.

Value

A list with the following elements:

beta Estimated fixed effects (regression coefficients).

u Estimated random effects (frailties) for each cluster.

theta Estimated variance of the random effects.

p_value P-value for testing the null hypothesis $H_0 : \theta = 0$ (no frailty).

See Also

[Ml_Cox](#), [logLikelihood_1](#), [logLikelihood_2](#)

| | |
|---------------|--|
| simulate_data | <i>Simulate clustered competing risks data with shared frailty</i> |
|---------------|--|

Description

This function simulates clustered time-to-event data under a competing risks framework with shared frailty and the possibility of random censoring. Cause 1 is modeled through an inversion method of the subdistribution function, and cause 2 is introduced when inversion fails.

Usage

```
simulate_data(
  G,
  Z = NULL,
  prop = 0.6,
  beta = NULL,
  theta = 0.5,
  cens = FALSE,
  pcens = 0.25,
  tau = 0.5
)
```

Arguments

| | |
|-------|--|
| G | A vector of group or cluster identifiers (length N). Each value indicates which cluster the individual belongs to. |
| Z | A matrix of covariates (dimensions N x p). Can be set to NULL if no covariates are used. |
| prop | Proportion of individuals susceptible to cause 1 (default: 0.6). |
| beta | A numeric vector of regression coefficients, one per covariate (length p). |
| theta | Variance of the shared frailty term for event times (cause 1). |
| cens | Logical, indicating whether censoring should be simulated (default: FALSE). |
| pcens | Target censoring proportion (default: 0.25). |
| tau | Variance of the shared frailty term for censoring times (default: 0). |

Value

A data.frame with one row per individual and at least the columns:

times Observed follow-up time.

status Event indicator: 0 for censoring, 1 for cause 1, 2 for cause 2.

clusters Cluster identifier.

If covariates are simulated, additional numeric covariate columns are included.

Examples

```
n_cov <- 1
n_cluster <- 5
n_per_cluster <- 100
n <- n_cluster * n_per_cluster

G <- rep(1:n_cluster, each = n_per_cluster)
Z <- matrix(runif(n * n_cov), ncol = n_cov)

df <- simulate_data(
  G = G,
  Z = Z,
  prop = 0.6,
  beta = c(0.5),
  theta = 0.01,
  cens = TRUE,
  pcens = 0.25,
  tau = 0.01
)

head(df)
table(df$status)
```

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